



An Old, New Idea

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LQG Autumn 2014



The Problem Pension long term return assumptions of 8 percent or even higher to estimate their actuarial liability.

The Idea Find sets of assets that have the property of co-integration relative to the return assumption as a fixed benchmark.

Deviations mean-revert Motivated by economic equilibrium theories linking assets prices or expected returns to fundamentals.



- ▶ MSCI developed equities (USD, Gross)
- ▶ Jan 1970 to July 2014
- ▶ Target of World + 7%
- ▶ Stock and Watson 1988 and diBartolomeo 1999
- ▶ Optimize every 4 years, quarterly rebalance, expanding window
- ▶ Adding a few objectives



$$\min f(w) \cong \left\{ \begin{array}{l} -\text{Co-integration Prob}(w) \\ \text{Surplus}(w) \\ \text{turnover}(w) * \mathbb{I}_{[\text{turnover}(w) \geq 40\%]} \end{array} \right\}$$

s.t.

$$0 \leq w_i \leq (.75, .5, .25)$$

$$\Sigma w = 1$$

$$.7 \leq (\beta * w) \leq 1.3$$

$$\Sigma \mathbb{I}_{[w \geq .05]} > 7$$

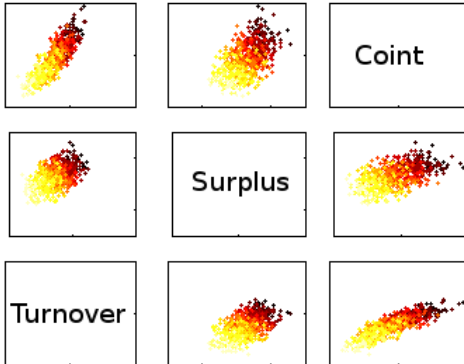
where

$$resids = w^T * P - Liab$$

$$Surplus = resids^T * resids / Liab^T * Liab$$



- Generate a Pareto Optimal frontier.





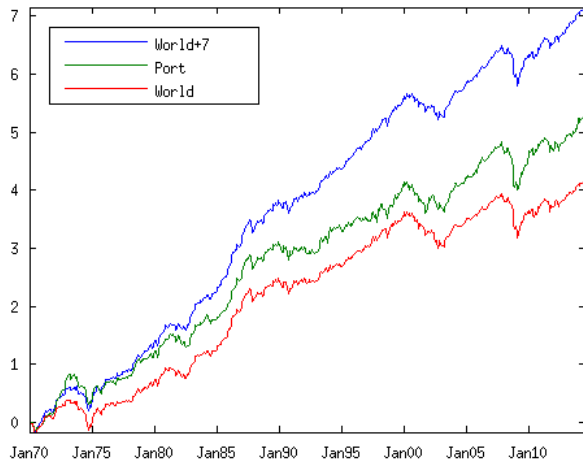
	wts	mkt	credit	indpro	slope	smb
JAPAN	0.253	0.948	-2.340	1.487	0.514	-0.204
USA	0.159	0.949	1.058	-0.517	-0.021	0.139
WORLDexUSA	0.116	1.035	-1.471	0.354	-0.339	-0.142
SINGAPORE	0.100	1.159	-3.884	0.006	-0.267	-0.246
PACIFIC	0.091	0.995	-2.044	1.264	-0.371	-0.196
CANADA	0.085	1.018	-1.316	-0.501	-3.304	-0.081
SWEDEN	0.063	0.766	-0.393	-0.997	-0.704	-0.094
WORLD	0.063	1.000	-0.000	0.000	0.000	-0.000
NETHERLANDS	0.031	0.992	-2.722	-0.401	1.032	-0.115
UK	0.016	1.294	1.418	-0.810	-1.054	-0.137
Exposures	1	1.004	-1.465	0.358	-0.265	-0.116
$XSec_{\sigma}$	0.065	0.212	1.733	1.054	1.827	0.129

Table : Portfolio Wts and Betas

Obligatory LQG chart



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	wts	mkt	credit	slope	smb	indpro
HONGKONG	0.220	1.155	-3.120	-1.111	-0.265	0.412
JAPAN	0.211	1.013	-0.508	-0.207	-0.106	0.047
SWEDEN	0.181	1.071	-2.360	-2.550	-0.129	-0.565
BELGIUM	0.121	0.932	-6.249	1.810	-0.168	-0.554
NETHERLANDS	0.104	1.011	-3.956	0.882	-0.101	-0.316
WORLDeXUSA	0.066	1.061	-1.526	-0.341	-0.109	-0.088
UK	0.056	1.093	-0.246	-0.021	-0.102	-0.318
EAFE	0.020	1.043	-1.306	-0.257	-0.120	-0.135
SINGAPORE	0.017	1.153	-4.942	-0.235	-0.168	0.146
FRANCE	0.009	1.095	-1.276	-1.531	-0.205	-0.469
Exposures	1	1.078	-2.636	-0.482	-0.155	-0.128
$XSec_{\sigma}$	0.072	0.119	2.268	1.325	0.090	0.290

Table : Portfolio Wts and Betas



	1989	1993	1997	2001	2005	2009	2013
mkt	1.004	1.061	1.086	1.094	1.058	1.078	1.064
hml	1.106	1.310	1.320	1.072	1.023	0.657	0.698
smb	2.467	1.785	1.853	1.774	1.769	1.463	1.388
mom	0.436	-0.131	0.364	-1.083	-0.825	-0.519	-1.341
ltr	-0.607	-1.212	-0.696	-0.423	-0.649	0.090	0.079
credit	-1.870	-1.410	-1.241	-1.152	-1.139	-0.411	-0.191
indpro	1.440	1.647	1.076	1.134	1.124	0.277	0.955
slope	1.782	2.015	1.847	1.817	2.312	1.784	1.162

Table : Portfolio Exposures



31-Dec-1969 to 31-Jul-2014

$R^2 = 0.7271$, $\bar{R}^2 = 0.7229$, $\sigma^2 = 0.0008$

Durbin-Watson 2.1456 , (Nobs, Nvars) (534, 9)

annualized Alpha: 3.04

variable	Coeff	t-stat	t-prob
const	0.002534	2.068	0.039
WORLD	1.074456	34.592	0.000
HML	-0.117181	-2.251	0.024
SMB	-0.142353	-3.002	0.002
MOM	0.004200	0.144	0.885
LTR	0.161108	2.687	0.007
Cred	-2.598261	-2.441	0.014
IP	-0.115500	-0.451	0.652
Slope	-0.127070	-0.166	0.867

Results Out of Sample



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29-Dec-1989 to 31-Jul-2014

$R^2 = 0.6809$, $\bar{R}^2 = 0.6720$, $\sigma^2 = 0.0013$

Durbin-Watson 2.169 , (Nobs, Nvars) (295, 9)

annualized Alpha: 2.182

variable	Coeff	t-stat	t-prob
const	0.001818	0.857	0.391
WORLD	1.145898	21.525	0.000
HML	-0.202181	-2.383	0.017
SMB	-0.189765	-2.326	0.020
MOM	0.009567	0.219	0.826
LTR	0.243743	2.302	0.022
Cred	-3.402299	-1.641	0.101
IP	-0.358242	-0.975	0.329
Slope	-0.162474	-0.095	0.924



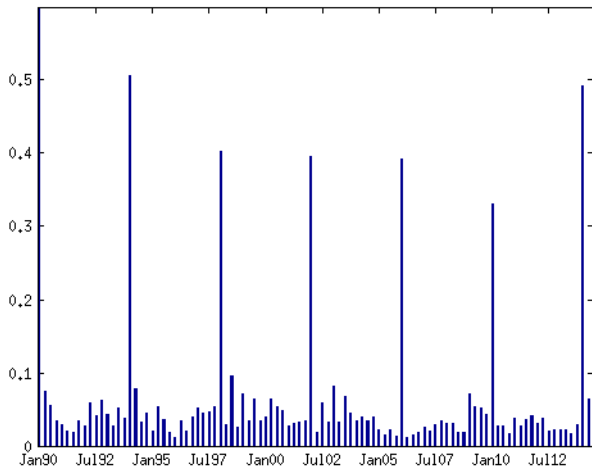
Post Crisis: 31-Jan-2007 to 31-Jul-2014

$R^2 = 0.7842$, $\bar{R}^2 = 0.7626$, $\sigma^2 = 0.0012$

Durbin-Watson 2.10 , (Nobs, Nvars) (89, 9)

annualized Alpha: 6.9942

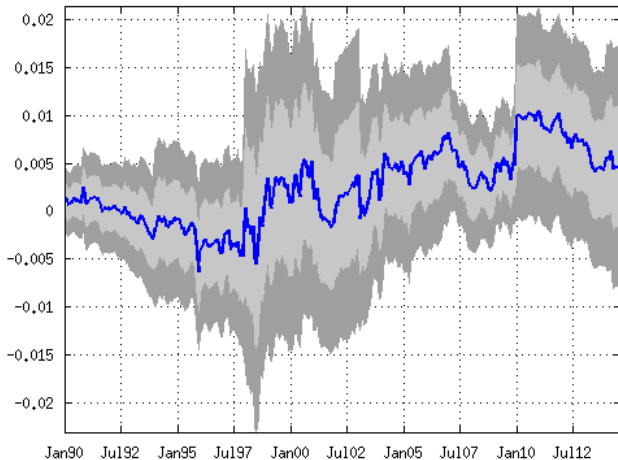
variable	Coeff	t-stat	t-prob
const	0.005829	1.517	0.133
WORLD	1.092282	10.716	0.000
HML	-0.733416	-3.332	0.001
SMB	-0.369407	-1.970	0.052
MOM	-0.084969	-1.112	0.269
LTR	0.680555	3.269	0.001
Cred	-6.702638	-2.365	0.020
IP	-0.102626	-0.214	0.830
Slope	-5.624491	-2.125	0.036



Factor Exposures: Rolling 5 yr α



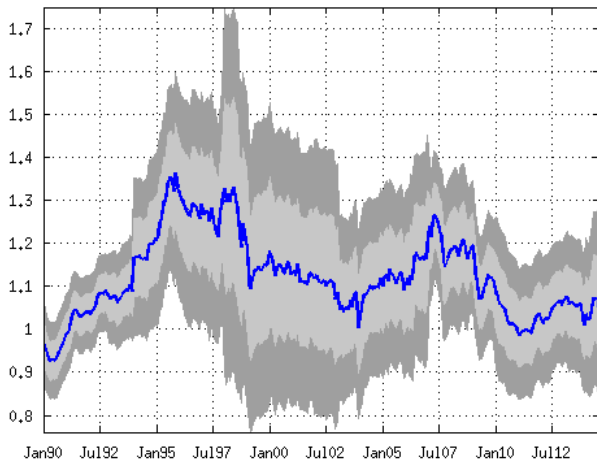
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Factor Exposures β



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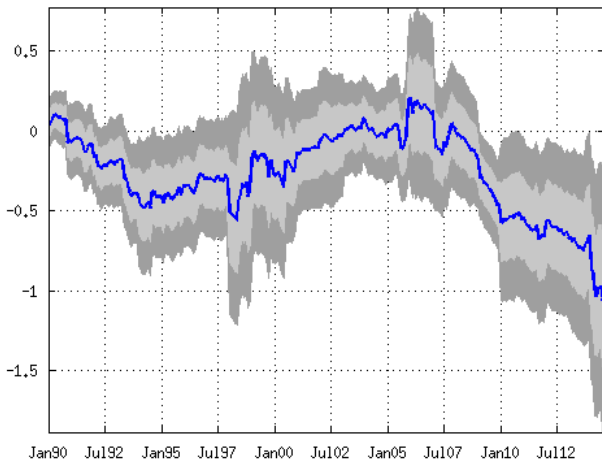


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Factor Exposures HML



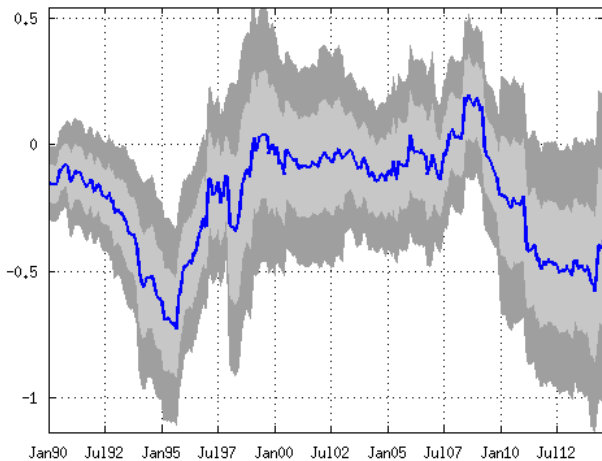
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Factor Exposures SMB



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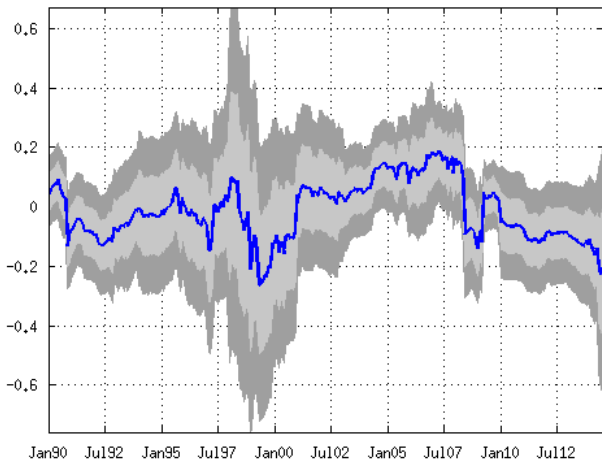


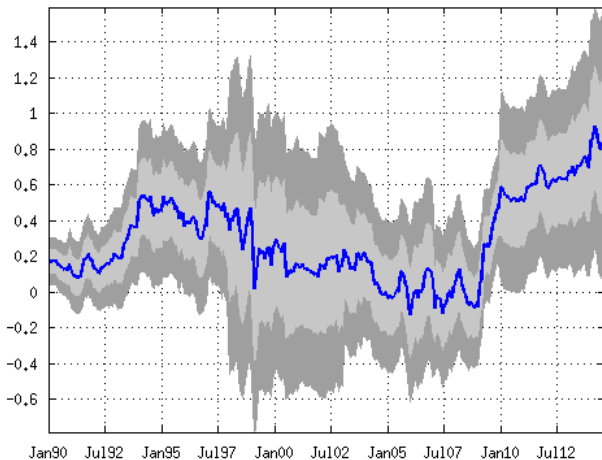
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Factor Exposures MOM



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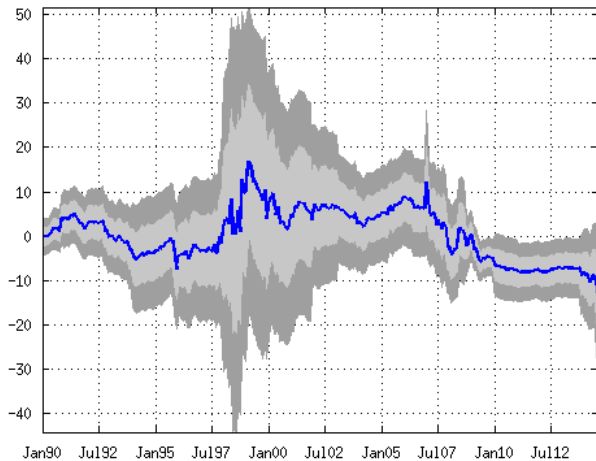




Factor Exposures Credit



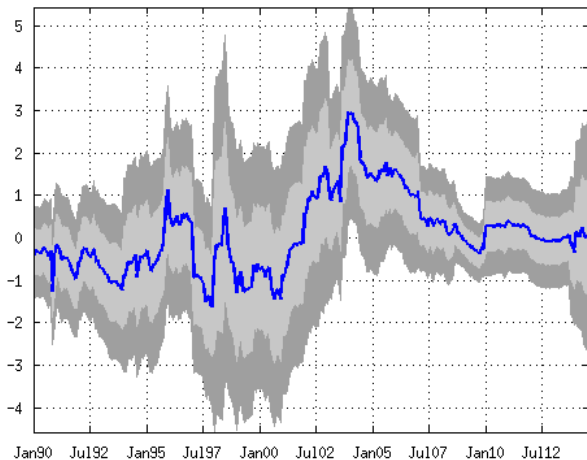
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Factor Exposures Ind Prod



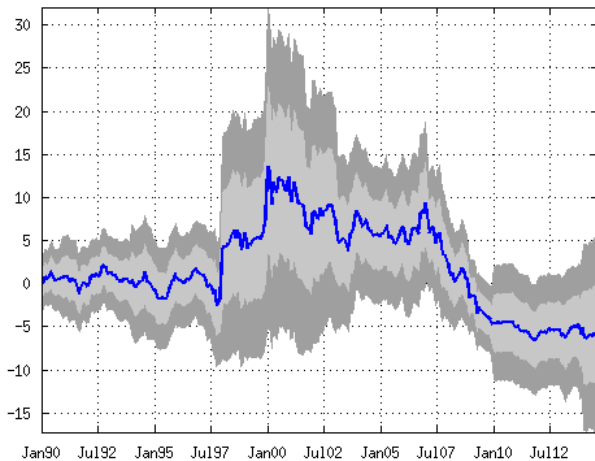
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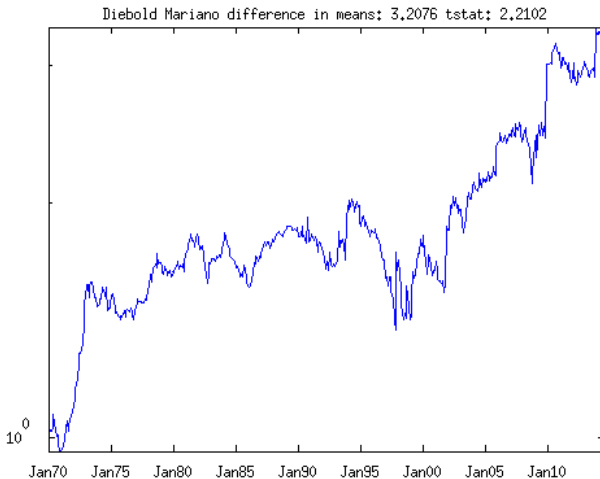


Factor Exposures Term Slope

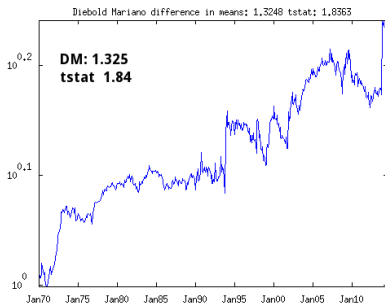


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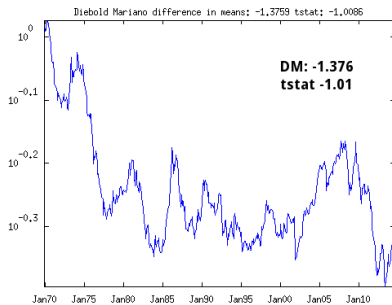




Diebold Mariano Diff in Means 3.2% t-stat 2.2



(a) World + 3%



(b) World - 7%

Figure : Two alternate drift targets



- ▶ Cointegrating relationship
- ▶ Market plus premia tilts
- ▶ Flexible optimization
- ▶ No convergence results



	wts	mkt	credit	slope	indpro	smb
HONGKONG	0.246	1.130	-3.342	-1.431	0.216	-0.258
SWEDEN	0.186	1.109	-2.776	-2.269	-0.687	-0.147
NETHERLANDS	0.114	1.031	-4.076	0.943	-0.485	-0.105
BELGIUM	0.107	0.938	-6.120	1.595	-0.608	-0.176
JAPAN	0.098	0.974	-0.019	-0.301	0.278	-0.097
SINGAPORE	0.073	1.133	-4.714	-0.711	0.053	-0.179
WORLDexUSA	0.068	1.063	-1.630	-0.372	-0.129	-0.109
EAFE	0.038	1.048	-1.450	-0.252	-0.179	-0.121
FRANCE	0.031	1.125	-1.861	-1.193	-0.656	-0.210
SWITZERLAND	0.023	0.886	-1.590	2.743	-0.138	-0.050
Exposures	1	1.064	-3.107	-0.591	-0.209	-0.166
$XSec_{\sigma}$	0.067	0.104	2.375	1.303	0.315	0.090

Table : Portfolio Wts and Betas



- ▶ Campbell J. and Shiller R. (2001) Valuation Ratios and the Long-Run Stock Market Outlook: An Update.
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